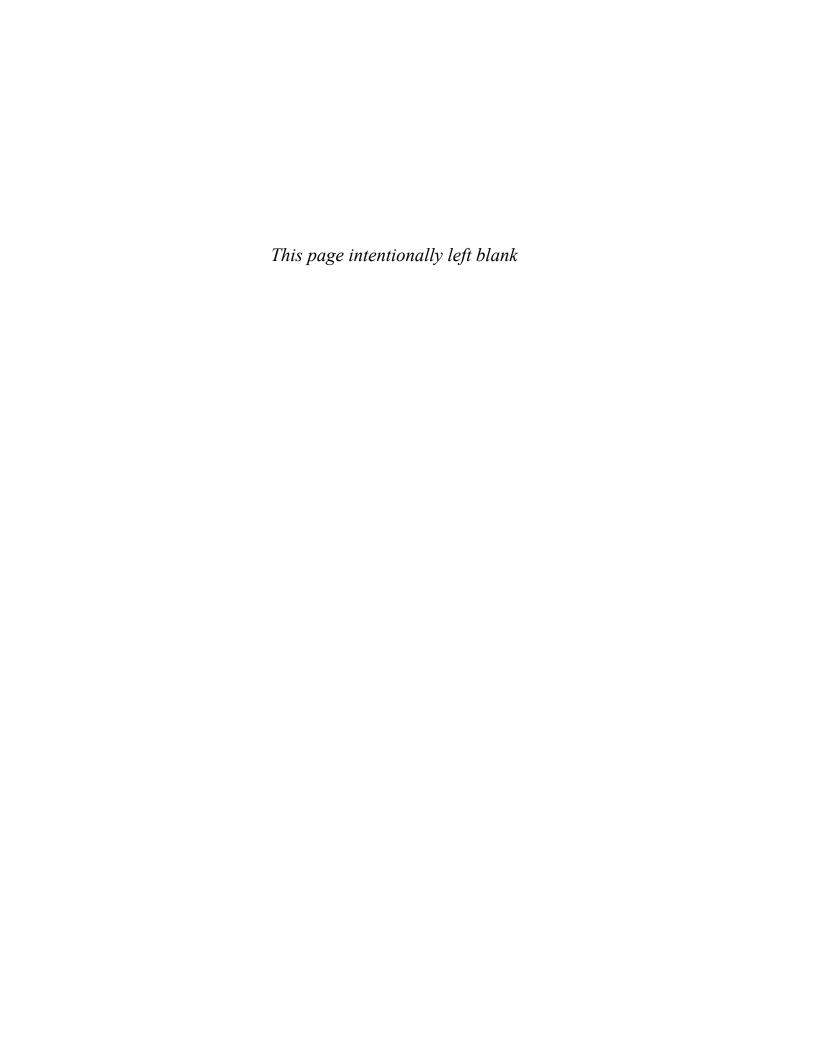
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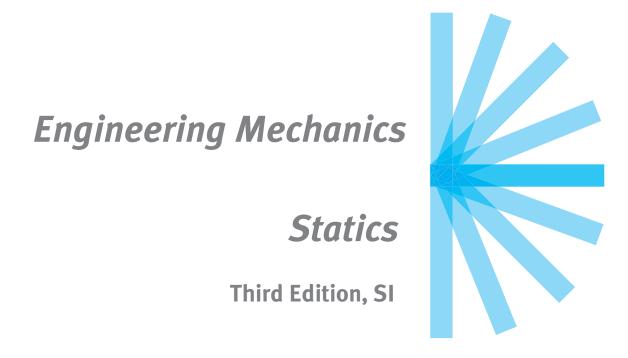
# ENGINEERING MECHANICS

# STATICS

**SOLUTION MANUAL** 

ANDREW PYTEL JAAN KIUSALAAS





# **SOLUTION MANUAL**





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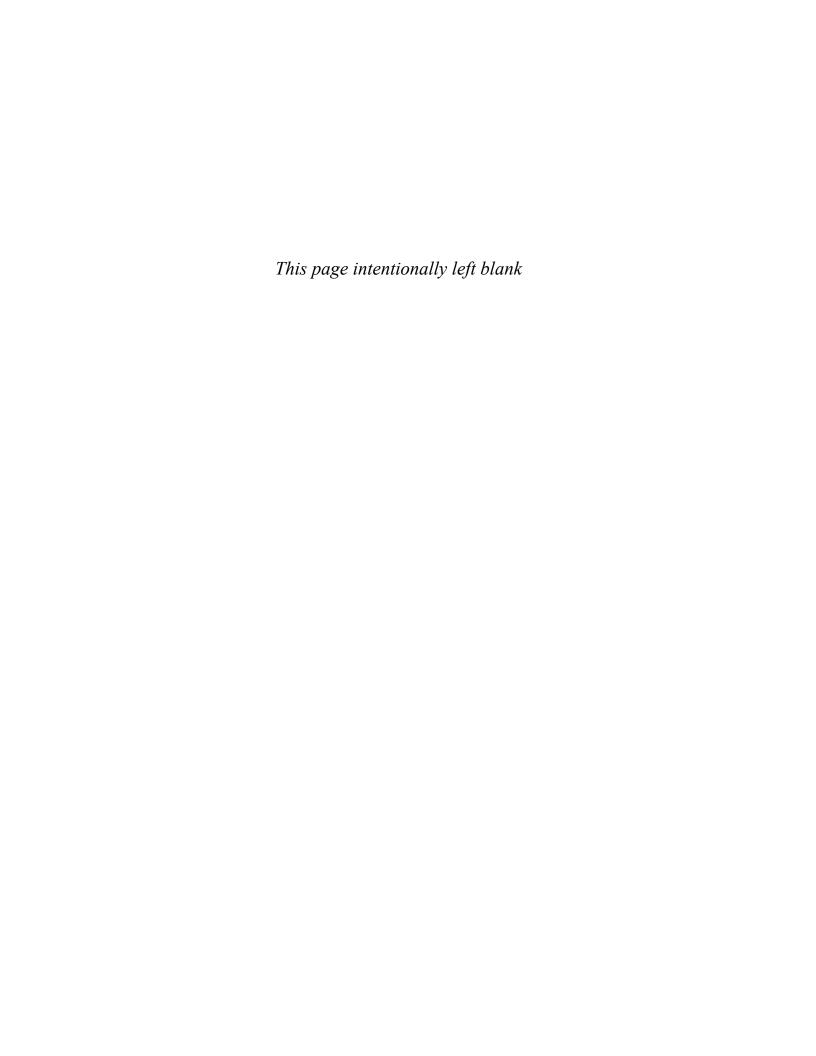
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## Chapter 1

1.1

(a) 
$$m = \frac{150 \text{ N}}{1.64} = 91.46 \text{ kg}$$

**(b)** W = mg = 
$$(91.46)(9.81) = 897.2 \text{ N}$$

1.2

W = 
$$\rho$$
 gV =  $(7850)(9.81)\pi(0.06)^2(0.120) = 104.51$  N  
W =  $mg$  104.51 =  $(m) \times 9.81$   $m = \frac{104.51}{9.81} = 1065$  kg

1.3

(a) 
$$40000 \text{ N} \cdot \text{cm} = 40000 \text{ N} \cdot \text{cm} \times \frac{1 \text{ kN}}{1000 \text{ N}} \times \frac{1 \text{ m}}{1000 \text{ m}} = 0.4 \text{ kN} \cdot \text{m}$$

(b) 1 bar = 
$$10^5 \text{Pa} = 10^5 \text{N/m}^2 \times \frac{1 \text{ kn/m}^2}{1000 \text{ N/m}^2} = 100 \text{kN/m}^2 = 100 \text{ kPa}$$

(c) 
$$6 \text{ m/s} = 6 \text{ m/s} \times \frac{1000 \text{ mm}}{1 \text{ m}} \times \frac{3600 \text{ s}}{1 \text{ m}} = 2.16 \times 10^7 \text{ mm/h}$$

(d) 
$$500 \text{ g/mm} = 500 \text{ g/mm} \times \frac{1 \text{ kg}}{1000 \text{ g}} \times \frac{1000 \text{ mm}}{1 \text{m}} = 500 \text{ g/m}$$

1.4

$$I = 1035285.8 \text{ g} \cdot \text{mm}^2 \times \frac{1 \text{ kg}}{(1000 \text{ g})} \times \frac{1 \text{m}^2}{(1000 \text{ mm})^2} = 1.0352858 \times 10^{-3} \text{kg} \cdot \text{m}^2$$

Rounding off to four significant digits

$$\therefore I = 1.035 \times 10^{-3} \text{kg} \cdot \text{m}^2 \blacklozenge$$

$$I = 1.35285.8 \times \frac{\text{kg}}{(1000 \text{ g})} \times \frac{\text{m}^2}{(1000 \text{ mm})^2} = 103.5 \times 10^{-5} \text{kg} \cdot \text{m}^2$$

The dimensions of 
$$\frac{\mathbf{gkx}}{\mathbf{W}}$$
 are:  $[\mathbf{g}][\mathbf{k}][\mathbf{x}] \left[\frac{1}{W}\right] = \left[\frac{L}{T^2}\right] \left[\mathbf{M}\mathbf{T}^{-2}\right] \left[\mathbf{L}\right] \left[\frac{1}{\mathbf{M}\mathbf{L}\mathbf{T}^{-2}}\right] = \left[\frac{\mathbf{L}}{\mathbf{T}^2}\right] = [\mathbf{a}]$  Q.E.D.

1.7

The dimensions of 
$$k = \frac{F}{x}$$
 are:  $[k] = \left[\frac{F}{x}\right] = \left[\frac{ML}{T^2}\right] \left[\frac{1}{L}\right] = \left[\frac{M}{T^2}\right] +$ 

1.8

(a) 
$$25 \text{ mm}/\mu s = \frac{25 \text{ mm}}{\mu s} \times \frac{1.0 \text{ m}}{1000 \text{ mm}} \times \frac{1.0 \mu s}{10^{-6} \text{ s}} = 25 000 \text{ m/s} \blacktriangleleft$$

1.9

$$y = kx^2$$
 (where  $k = 1.0$ )

The dimensions of 
$$k = \frac{y}{x^2}$$
 are:  $\therefore [k] = \left[\frac{y}{x^2}\right] = \left[\frac{L}{L^2}\right] = \left[\frac{1}{L}\right]$ 

 $y = x^2$  can be dimensionally correct if the units of the constant 1.0 (not shown explicity) are understood to be m<sup>-1</sup>

$$[I] = \left[ mR^2 \right] = \left[ ML^2 \right] \quad \blacklozenge$$

(a) The dimensions of  $x = At^2 - Bvt$  are

$$[L] = [A][T^2] - [B][LT^{-1}][T]$$
  
 $\therefore [A] = [LT^{-2}] \blacktriangleleft [B] = [1] \text{ (dimensionless)} \blacktriangleleft$ 

(b) The dimensions of  $x = Avte^{-Bt}$  are

$$\begin{array}{lll} [L] & = & [A][LT^{-1}][T]e^{[B][T]} \\ [B][T] & = & [1] & \therefore [B] = [T^{-1}] \blacktriangleleft \\ [L] & = & [A][LT^{-1}][T] & \therefore [A] = [1] \blacktriangleleft \\ \end{array}$$

$$\begin{bmatrix} \mathbf{m} \frac{\mathbf{d}^2 \mathbf{x}}{\mathbf{d}t^2} \end{bmatrix} = [\mathbf{m}] \qquad \begin{bmatrix} \frac{\mathbf{L}}{\mathbf{T}^2} \end{bmatrix} = [\mathbf{M}L\mathbf{T}^{-2}] \quad \text{Therefore, the dimension of each term is } [\mathbf{M}L\mathbf{T}^{-2}] \\ \begin{bmatrix} \mathbf{c} \frac{\mathbf{d} \mathbf{x}}{\mathbf{d}t} \end{bmatrix} = [\mathbf{c}] \begin{bmatrix} \frac{\mathbf{L}}{\mathbf{T}} \end{bmatrix} = [\mathbf{M}L\mathbf{T}^{-2}] \quad \therefore \quad [\mathbf{c}] = [\mathbf{M}\mathbf{T}^{-1}] \quad & \\ [\mathbf{k}\mathbf{x}] = [\mathbf{k}][\mathbf{L}] = [\mathbf{M}L\mathbf{T}^{-2}] \quad & \therefore \quad [\mathbf{k}] = [\mathbf{M}\mathbf{T}^{-2}] \quad & \\ \begin{bmatrix} \mathbf{P}_0 \sin \omega t \end{bmatrix} = \begin{bmatrix} \mathbf{P}_0 \end{bmatrix} [\sin \omega t] = [\mathbf{M}L\mathbf{T}^{-2}] \\ & \therefore \quad [\mathbf{P}_0] = [\mathbf{M}L\mathbf{T}^{-2}] \quad & \\ & \omega t \end{bmatrix} = [\boldsymbol{\omega}][\mathbf{T}] = [\mathbf{1}] \quad & \therefore \quad [\boldsymbol{\omega}] = \begin{bmatrix} \mathbf{T}^{-1} \end{bmatrix} \quad & \\ & \vdots \quad & \\ &$$

From Eq. (11.17): 
$$G = \frac{FR^2}{m_A m_B}$$
 which gives  $[G] = \frac{[F][R^2]}{[m_A][m_B]}$  (1)  
Dim  $R^2 = [L^2]$  (2)

For an absolute system of units: Dimension  $F = \left\lceil \frac{ML}{T^2} \right\rceil$  and [m] = [M]

From Eqs. (1) and (2), we obtain  $[G] = \left[\frac{ML}{T^2}\right] \left[\frac{[L^2]}{[M][M]}\right] = \left[M^{-1}L^3T^{-2}\right]$ 

1.14

120 hp = 120 hp 
$$\times \frac{0.7457 \text{ kW}}{1.0 \text{ hp}} = 89.5 \text{ kW} \blacktriangleleft$$

$$F = G \frac{m_A m_B}{R^2} = \left(6.67 \times 10^{-11}\right) \frac{(10)(10)}{(0.5)^2} = 2.668 \times 10^{-8} \text{ N}$$

$$W = mg = (10)(9.81) = 98.1 \text{ N}$$

% of weight = 
$$\frac{F}{W} \times 100\% = \frac{2.668 \times 10^{-8}}{98.1} \times 100\% = 2.72 \times 10^{-8}\%$$

$$\mathbf{F} = \mathbf{G} \frac{\mathbf{m_A} \mathbf{m_B}}{\mathbf{R^2}} = (6.67 \times 10^{-11}) \times \frac{(2)(2)}{\left(\frac{160}{1000}\right)^2} = 1.042 \times 10^{-8} \,\text{N} \quad \blacklozenge$$

1.17

$$h = 9000 \text{ m} = 9 \text{ km}$$

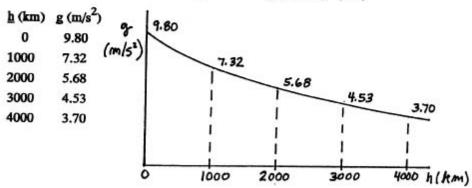
On earth: 
$$W_{\epsilon} = \frac{GM_{\epsilon}m}{R_{\epsilon}^2}$$
 At elevation  $h$ :  $W = \frac{GM_{\epsilon}m}{(R_{\epsilon} + h)^2}$  
$$W = W_{\epsilon} \frac{R_{\epsilon}^2}{(R_{\epsilon} + h)^2} = 900 \frac{6378^2}{(6378 + 9)^2} = 897.5 \text{ N}$$

1.18

$$\begin{array}{lll} g_m & = & \frac{GM_m}{R_m^2} & g_e = \frac{GM_e}{R_e^2} \\ \\ \frac{g_m}{g_e} & = & \frac{M_m R_e^2}{M_e R_m^2} = \frac{0.07348(6378)^2}{5.974(1737)^2} = 0.1658 \approx \frac{1}{6} \text{ Q.E.D.} \end{array}$$

1.19

Shown below is the plot of 
$$g = \frac{GM_e}{R^2} = \frac{(6.67 \times 10^{-11})(5.9742 \times 10^{24})}{(6378 + h)^2 (10^6)}$$



On earth: 
$$W_{\rm e}=\frac{GM_{\rm e}m}{R_{\rm e}^2}$$
 At elevation  $h$ :  $W=\frac{GM_{\rm e}m}{(R_{\rm e}+h)^2}$ 

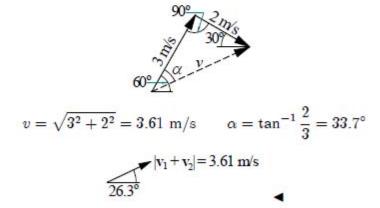
$$W = \frac{W_e}{10} \frac{GM_em}{(R_e + h)^2} = \frac{GM_em}{10R_e^2} \qquad (R_e + h)^2 = 10R_e^2$$

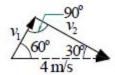
$$(6378 + h)^2 = 10(6378)^2 \qquad h = 13790 \text{ km} \blacktriangleleft$$

$$R = R_e + R_m + d = 6378 + 1737 + 384 \times 10^3$$
  
=  $392.1 \times 10^3 \text{ km} = 392.1 \times 10^6 \text{ m}$ 

$$F = G \frac{M_e M_m}{R^2} = (6.67 \times 10^{-11}) \frac{(5.974 \times 10^{24}) (0.07348 \times 10^{24})}{(392.1 \times 10^6)^2}$$
$$= 1.904 \times 10^{20} \text{ N} \blacktriangleleft$$

#### 1.22





$$v_1 = 4 \sin 30^\circ = 2 \text{ m/s} \quad \blacktriangleleft \quad v_2 = 4 \sin 60^\circ = 3.46 \text{ m/s} \quad \blacktriangleleft$$

Horizontal: 
$$H = 6250 \sin 6^\circ = 653 \text{ N} (\rightarrow)$$

Vertical: 
$$V = 6250 \cos 6^{\circ} = 6220 \,\text{N}$$
 (†) •



#### 1.25

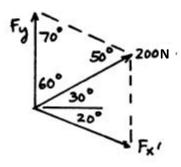
(a) 
$$F_x = 200 \cos 30^\circ = 173.2 \text{ N}$$

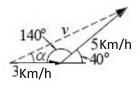
(a) 
$$F_x = 200 \cos 30^\circ = 173.2 \text{ N} \quad \Leftrightarrow \quad F_y = 200 \sin 30^\circ = 100.0 \text{ N} \quad \uparrow \quad \Leftrightarrow$$

(b) Law of sines: 
$$\frac{200}{\sin 70^{\circ}} = \frac{F_y}{\sin 50^{\circ}} = \frac{F_{x'}}{\sin 60^{\circ}}$$
which gives

$$F_y = \frac{200 \sin 50^\circ}{\sin 70^\circ} = 163.0 \text{ N}$$

$$F_{x'} = \frac{200 \sin 60^{\circ}}{\sin 70^{\circ}} = 184.3 \text{ N} \quad \blacklozenge$$





Law of cosines: 
$$v = \sqrt{3^2 + 5^2 - 2(3)(5)\cos 140^\circ} = 7.549 \text{ Km/h}$$

Law of cosines: 
$$v = \sqrt{3^2 + 5^2 - 2(3)(5)\cos 140^\circ} = 7.549 \text{ Km/h}$$
Law of sines:  $\frac{5}{\sin \alpha} = \frac{7.549}{\sin 140^\circ} = 0.4257$   $\alpha = 25.2^\circ$ 

Geometry: 
$$\alpha = \tan^{-1} 0.5 = 26.57^{\circ}$$

$$2\alpha + \gamma = 90^{\circ}$$
 from which

$$\gamma = 90^{\circ} - 2(26.57^{\circ}) = 36.86^{\circ}$$

Law of cosines:

$$R = \sqrt{76^2 + 52^2 - 2(76)(52)\cos 36.86^{\circ}}$$

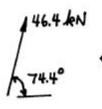
Law of sines : 
$$\frac{R}{\sin \gamma} = \frac{Q}{\sin \theta}$$
 which gives

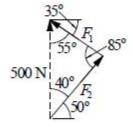
$$\theta = \sin^{-1} \left[ \frac{Q \sin \gamma}{R} \right] = \sin^{-1} \left[ \frac{52 \sin 36.86^{\circ}}{46.43} \right] = 42.21^{\circ}$$

Geometry: 
$$\beta = 180^{\circ} - \theta - \gamma - \alpha$$

$$= 180^{\circ} - 42.21^{\circ} - 36.86^{\circ} - 26.57^{\circ} = 74.4^{\circ}$$

Therefore, the resultant of P and Q is:

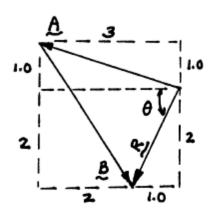




Law of sines: 
$$\frac{500}{\sin 85^{\circ}} = \frac{F_1}{\sin 40^{\circ}} = \frac{F_2}{\sin 55^{\circ}}$$

$$\therefore F_1 = \frac{500 \sin 40^{\circ}}{\sin 85^{\circ}} = 323 \text{ N} \blacktriangleleft$$

$$F_2 = \frac{500 \sin 55^{\circ}}{\sin 85^{\circ}} = 411 \text{ N} \blacktriangleleft$$

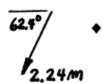


#### R = A + B

By inspection of the triangle (dimensions in meters

$$R = \sqrt{2^2 + 1.0^2} = 2.24 \text{ m} \text{ and } \theta = \tan^{-1} 2 = 62.4^{\circ}$$

Therefore, the resultant of A and B is:



#### 1.30

$$R = P + Q$$

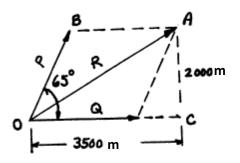
$$P = \frac{2000}{\sin 65^{\circ}} = 2207 \, \text{m}$$

$$Q = 3500 - P\cos 65^{\circ}$$

$$= 3500 - 2207\cos 65^{\circ} = 2567 \text{ m}$$

Therefore, the components are:

2210 ft along OB and 2570m along OC ◆



#### 1.31

Law of sines: 
$$\frac{360}{\sin 95^{\circ}} = \frac{P_{AB}}{\sin 30^{\circ}} = \frac{P_{AC}}{\sin 55^{\circ}}$$

which gives

$$P_{AB} = \frac{360 \sin 30^{\circ}}{\sin 95^{\circ}} = 180.7 \,\text{N}$$

$$P_{AC} = \frac{360 \sin 55^{\circ}}{\sin 95^{\circ}} = 296 \,\text{N}$$

